\mathbb{H} COLLEGE

Sem 1 Examination 2010 Question/answer booklet



MATHEMATICS: SPECIALIST 3CDMAS

Section Two (calculator-assumed)

Name:			
Teacher:			

Time allowed for this section

Section Two

Reading time before commencing work:

Working time for paper:

10 minutes

100 minutes

Material required/recommended for this paper

To be provided by the supervisor

Question/answer booklet for Section Two and a formula sheet (from Curriculum Council) which was provided with Section One.

To be provided by the candidate

Section Two:

Standard items:

pens, pencils, pencil sharpener, highlighter, eraser, ruler

Special items:

drawing instruments, templates, and up to three calculators, (CAS, graphic or scientific), which satisfy the conditions set by the Curriculum Council for this course. Up to two (2) A4 pages of notes (handwritten, photocopied or typed on both sides) that may be either personally or commercially produced. It must not be folded,

have anything stuck to it or have correction fluid/tape on it.

Important note to candidates

No other items may be taken into the examination room. It is your responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor before reading any further.

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Suggested working time (minutes)	Marks available
Section One: Calculator-free	7	7	50	39
Section Two: Calculator-assumed	13	13	100	79
-				118

Instructions to candidates

- 1. The rules for the conduct of Western Australian examinations are detailed in the *Year 12 Information Handbook 2010*. Sitting this examination implies that you agree to abide by these rules.
- 2. Answer the questions according to the following instructions.

Section Two: Write answers in this Question/Answer Booklet. **All** questions should be answered.

Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.

It is recommended that you do not use pencil except in diagrams.

- 3. You must be careful to confine your responses to the specific questions asked and to follow any instructions that are specific to a particular question.
- 4. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
- Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
- Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question(s) that you are continuing to answer at the top of the page.

MARK ALLOCATION AND RECORDS:

Section	Question	Marks	Awarded
TWO	8	3	
	9	3	
	10	4	
	11	4	
	12	4	
	13	4	
	14	5	
	15	5	
	16	5	
	17	6	
	18	8	
	19	10	
	20	18	
	Penalties	- 1/2/3	
	TWO	79	

Rounding (-1)	
Rounding (-1)	l
Units (-1)	
Notation (-1)	

Section Two: Calculator - 79 marks

This section has thirteen (13) questions. Attempt all questions.

Working time: 100 minutes

8. [3 marks]

Sketch the set of complex number z which satisfy the following condition

$$|z-4-2i| \le |\sqrt{2}+i\sqrt{2}|$$
.

9.[3 marks]

Use the ordinary rules of algebra to solve $\frac{z-i}{z+i}=1+i$ for z . (i.e. don't substitute z=x+yi)

10. [4 marks]

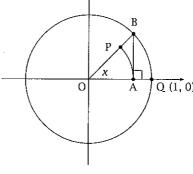
Find the derivative of $y = x - x^3$ from first principles.

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[4 marks]					
[4 marks] Find the exact di	stance betwee	n A (5, 140°) a	and B (8, -160)°).	
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[4 marks] Find the exact di	stance betwee	n A (5, 140°) a	and B (8, -160)*).	
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14.	[5	marks	
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Use de Moivre's rule to find the exact value of $(1 + i)^5 - (1 - i)^5$. 15.[5 marks] Find $\int_0^{\frac{\pi}{3}} \cos^2 \theta \sin^3 \theta \ d\theta$ exactly by letting $u = \cos \theta$. 16. [5 marks] Consider the unit circle shown. Use the fact that line AB Q (1, 0) $x \cos x < \sin x < x$ and hence that $\lim_{x\to 0} \frac{\sin x}{x} = 1$.

length of < length of < length of arc AP to establish that



***	$\int z d\theta = \int \operatorname{Re} z d\theta .$
7	,5 marks]
(a)	Show how to solve $w^3 = -2 + 2i$ for one solution of w in exact cartesian form.
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	Show how to solve $w^3 = -2 + 2i$ for one solution of w in exact cartesian form. Use your answer above to solve the equation below for one solution of z without substitution of $z = x + yi$.
	Use your answer above to solve the equation below for one colution
	Use your answer above to solve the equation below for one solution of z without substitution of $z = x + yi$.
(a) b)	Use your answer above to solve the equation below for one solution of z without substitution of $z = x + yi$.
	Use your answer above to solve the equation below for one solution of z without substitution of $z = x + yi$.
	Use your answer above to solve the equation below for one solution of z without substitution of $z = x + yi$.

19. [1,2,3,2,2 marks	19.	El,	2,3	5, 2	, 2	marks
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z and *w* are complex numbers such that z=1 - i and $w=2e^{i\frac{\pi}{6}}$. Find the following:

z	
w in exact cartesian form	
<i>zw</i> in exact polar form	
$\frac{w}{z^2}$ in exact exponential form	
z ⁵ in exact polar form.	

20. [7,11 marks]

A jet travelling at $\langle -200, 150, 0.5 \rangle$ km/hr passes through point (50, -20, 3.8) km at 2pm one day. At the same time a light plane is at (-238, 460, 4.52) km travelling at $\langle -80, -50, 0.2 \rangle$ km/hr.

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